

ALP Dark Matter: Beyond the Standard Paradigm

Based on 2206.14259, 2207.10111, 2305.03756, 23xx.xxxxx

Cem Eröncel, Istanbul Technical University

International Conference on Particle Physics and Cosmology (dedicated to Prof. Rubakov memory)

In collaboration with Aleksandr Chatrchyan (DESY → Stockholm), Matthias Koschnitzke (DESY), Géraldine Servant (DESY), Philip Sørensen (Padova) and Ryosuke Sato (Osaka)

Funded by the 2236 Co-Funded Brain Circulation Scheme2 (CoCirculation2) of The Scientific and Technological Research Council of Turkey TÜBİTAK (Project No: 121C404).

QCD Axion and Axion-Like-Particles (ALPs)

An “axion-like-particle (ALP)” is defined as a **scalar field** ϕ with the following **effective** Lagrangian at low energies:

$$\mathcal{L}_{\text{ALP}} = -\frac{1}{2}\partial_\mu\phi\partial^\mu\phi - \Lambda_b^4(T) \left[1 - \cos\left(\frac{\phi}{f_\phi}\right) \right] - \frac{g_{\phi\gamma}}{4}\phi F_{\mu\nu}\tilde{F}^{\mu\nu} + \dots$$

The mass (barrier-height) is in general **temperature-dependent**:

$$\Lambda_b^4(T) \approx m_\phi^2 \times \begin{cases} \left(\frac{T_c}{T}\right)^\gamma & , T \geq T_c \\ 1 & , T < T_c \end{cases}$$

QCD axion

$m_\phi^2 f^2 \approx (76 \text{ MeV})^4$, $\gamma \approx 8$, $T_c \approx 150 \text{ MeV}$
Couplings to photons, nucleons, electrons, etc...

Generic ALP

m_ϕ, f, γ, T_c are **free** parameters.
Might not have any coupling to SM.

This talk: A generic ALP with a **constant** mass, i.e. $\gamma = 0$.

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ALP dark matter: The standard paradigm

The cosmology of an ALP field ϕ is determined by the evolution equation:

$$\ddot{\phi} + 3H\dot{\phi} - \frac{\nabla^2}{a^2}\phi + V'(\phi) = 0, \quad V(\phi, T) = m_\phi^2(T)f_\phi^2 \left[1 - \cos\left(\frac{\phi}{f_\phi}\right) \right].$$

One also needs to specify the **initial conditions** that depends on the time of the **symmetry breaking** that has generated the ALP as the **pNGB**.

- **Post-inflationary:** Different initial conditions in each Hubble patch. **Inhomogeneous**.
- **Pre-inflationary:** Random initial angle $\theta \equiv \phi/f_\phi \in [-\pi, \pi)$ in observable universe. **Homogeneous**.

Assuming pre-inflationary scenario and **negligible** initial kinetic energy

$$\rho_\phi \propto \begin{cases} \text{constant}, & m(T) \ll H(T) \\ a^{-3}, & m(T) \gg H(T) \end{cases}.$$

The relic density for ALP dark matter is determined by $0 \leq |\theta_i| < \pi$.

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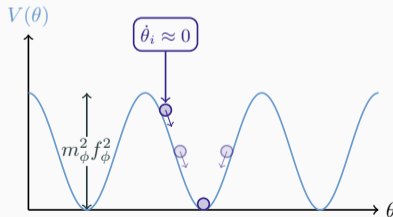
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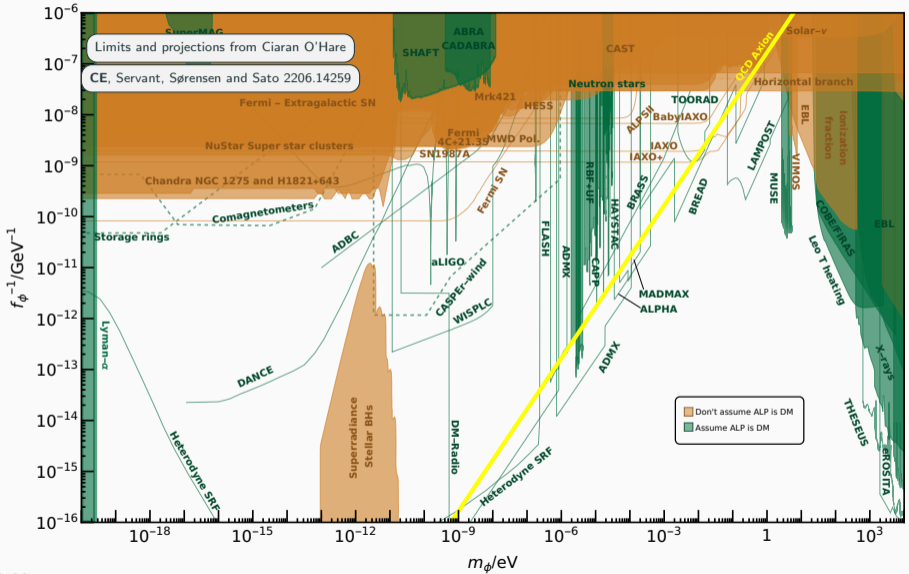
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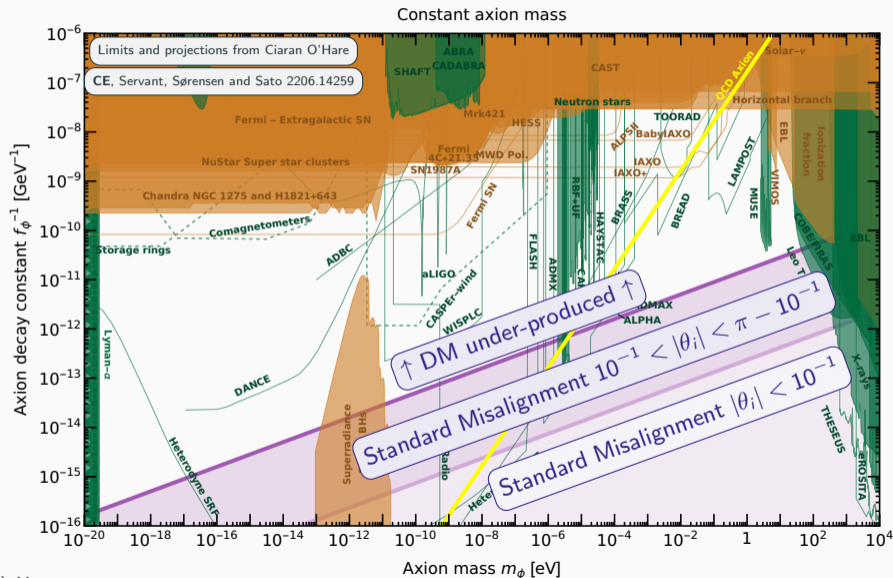
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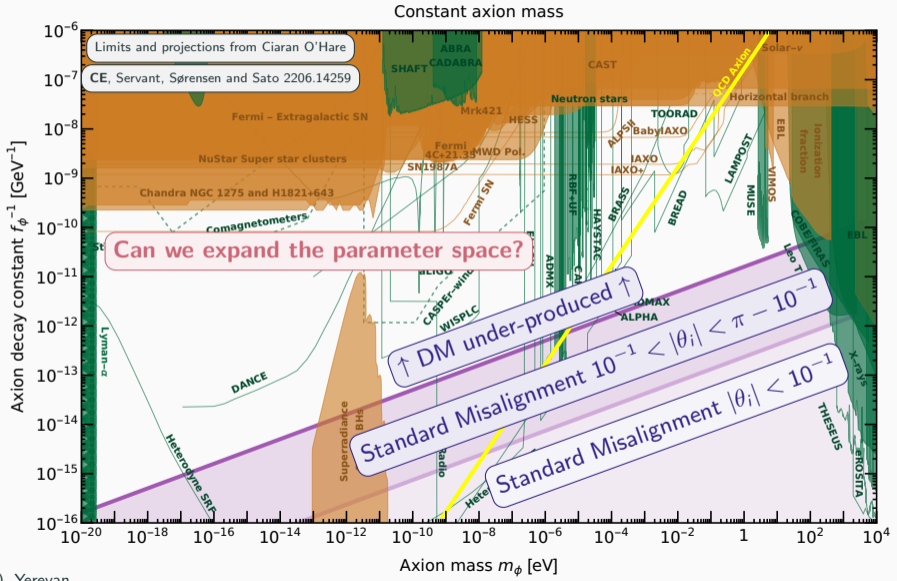
ALP dark matter parameter space in the standard paradigm (with $g_{\theta\gamma} = (\alpha_{em}/2\pi)(1.92/f_\phi)$)



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- Modify the initial conditions

- **Large misalignment:** Choose the initial angle very close to the top, i.e. $|\pi - \theta_i| \ll 1$.

Zhang, Chiueh 1705.01439; Arvanitaki et al. 1909.11665

- **Kinetic misalignment:** Start with a large initial kinetic energy.

Co et al. 1910.14152; Chang et al. 1911.11885

- Modify the potential to a non-periodic one:

Ollé+. 1906.06352; Chatrchyan, CE, Koschnitzke, Servant 2305.03756

$$V(\theta) = \frac{m_\phi^2 f_\phi^2}{2p} \left[(1 + \theta^2)^p - 1 \right], \quad p < 1.$$

Extending the parameter space to lower f_ϕ values

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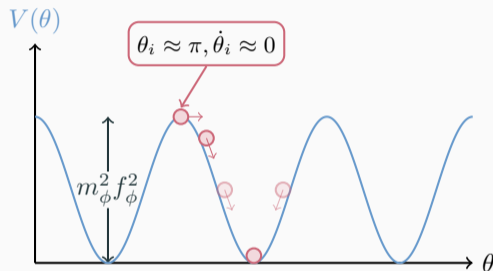
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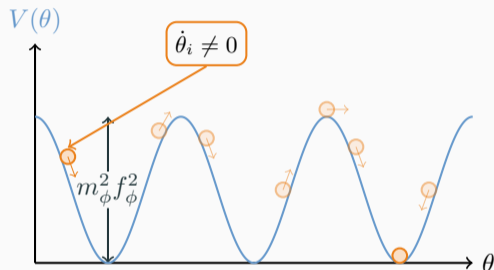
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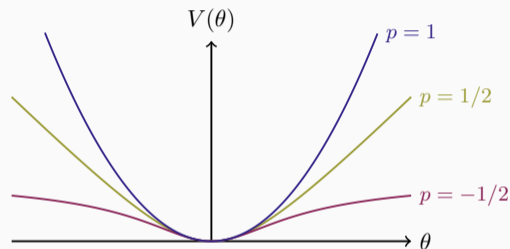
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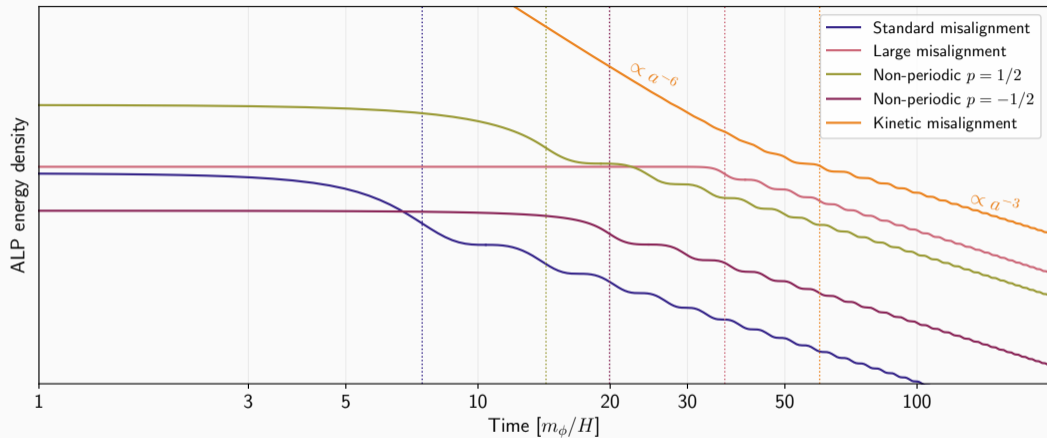
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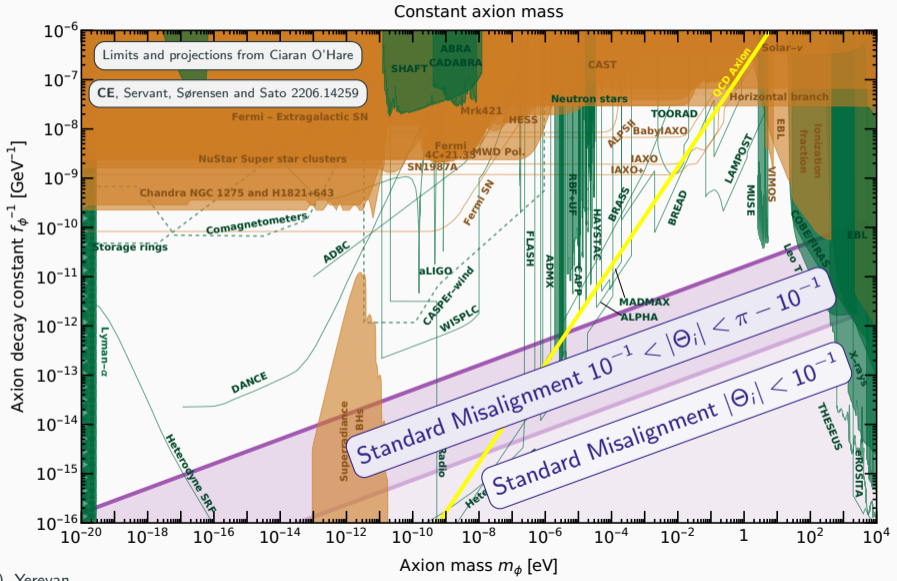


Expanding the parameter space to lower f_ϕ values

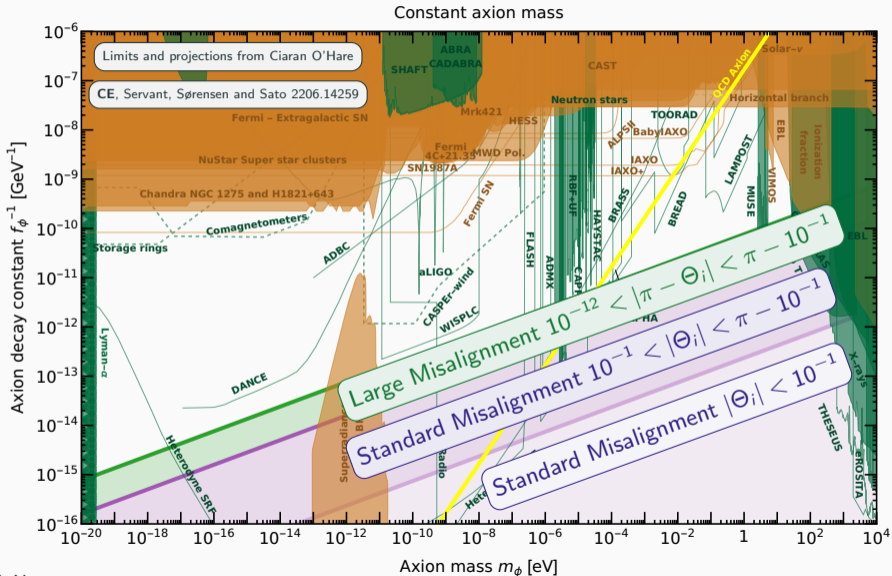


Common property of all these is that the onset of oscillations got **delayed** which **boosts** the dark matter abundance, and extends the ALP dark matter parameter space to **lower** decay constants.

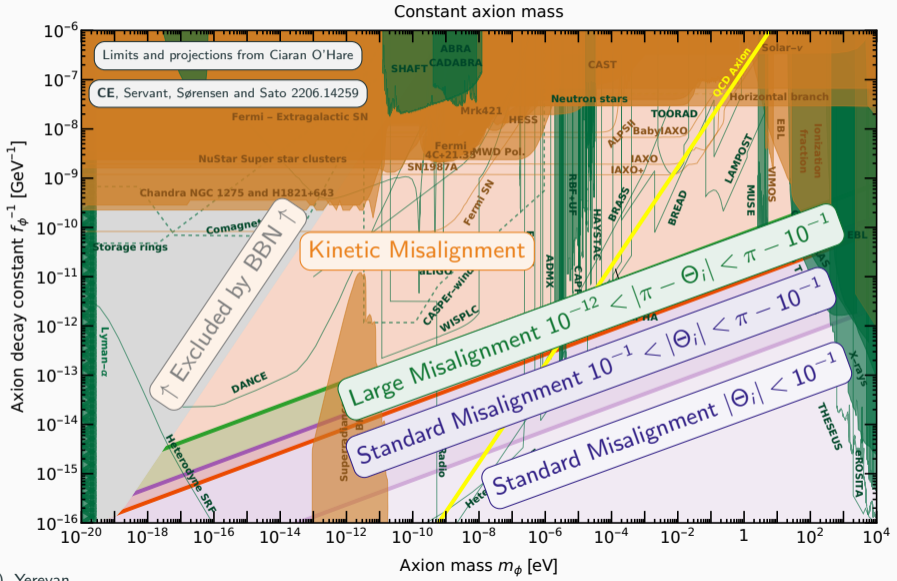
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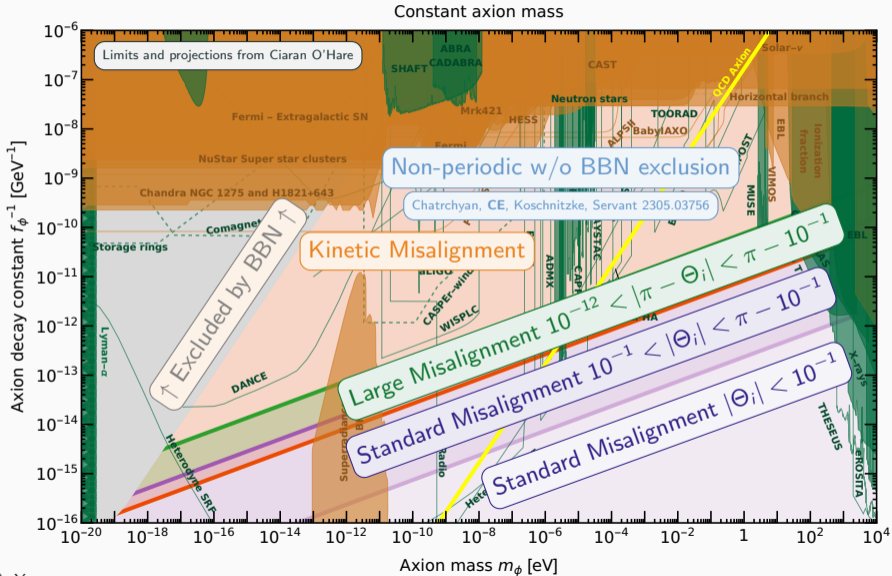
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How to get a large initial kinetic energy?

A large initial kinetic energy for the ALP field can be **motivated** in various UV completions:

- **Explicit** breaking of the PQ symmetry at very large energies. [Co et al. 1910.14152](#); [2004.00629](#); [2006.05687](#)
- **Trapped misalignment** [Luzio et al. 2102.00012](#); [2102.01082](#)

Today's ALP energy density is [Co et al. 1910.14152](#)

[CE, Servant, Sørensen, Sato 2206.14259](#)

$$h^2\Omega_{\phi,0} \approx 0.12 \left(\frac{m_\phi}{5 \times 10^{-3} \text{ eV}} \right) \left(\frac{Y}{40} \right), \quad Y = \frac{f_\phi \dot{\phi}(T)}{s(T)}$$

The **yield** parameter Y is conserved after the kick, and determines the ALP relic density today.

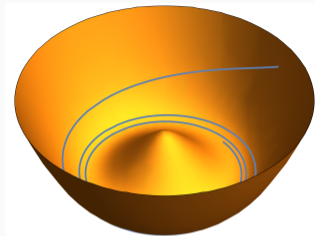
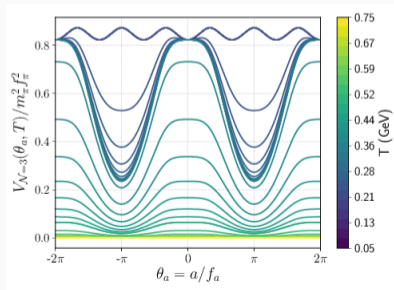


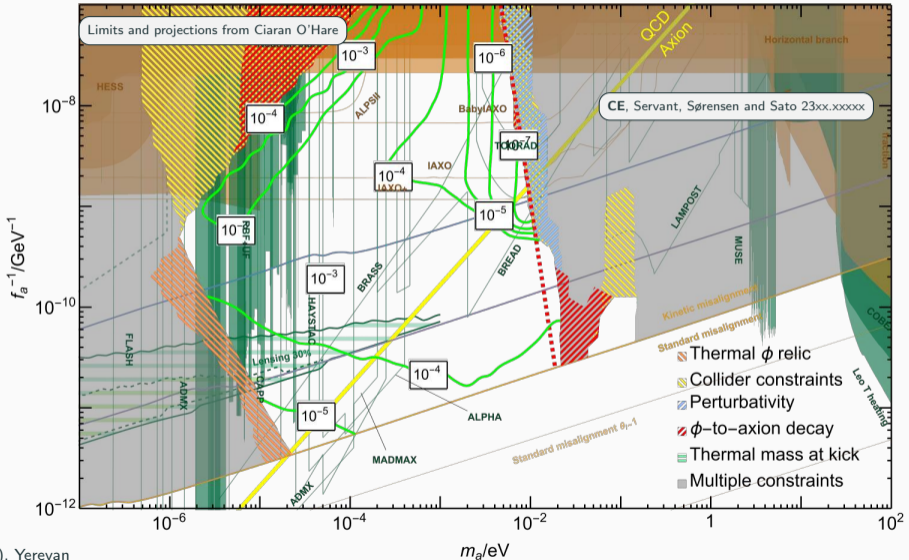
Figure credit: Philip Sørensen



[Luzio et al. 2102.01082](#)

Specific example of a UV completion with KSVZ fermions and nearly-quadratic potential

Yukawa: Necessary $A_s(k_{\text{kin}})$ suppression for $M=m_{\text{Pl}}$ and $n=13$



Fluctuations of the ALP field

Even in the pre-inflationary scenario ALP field has some **fluctuations** on top of the homogeneous background, that are seeded by the **adiabatic** and/or **isocurvature** perturbations.

$$\phi(t, \mathbf{x}) = \bar{\phi}(t) + \int \frac{d^3 k}{(2\pi)^3} \phi_k e^{i\vec{k}\cdot\vec{x}} + \text{h.c.}$$

The EoM for the **unavoidable adiabatic** perturbations are

$$\ddot{\phi}_k + 3H\dot{\phi}_k + \underbrace{\left[\frac{k^2}{a^2} + V''(\phi) \Big|_{\bar{\phi}} \right]}_{\text{eff. frequency}} \phi_k = \underbrace{2\Phi_k V'(\phi) \Big|_{\bar{\phi}} - 4\dot{\Phi}_k \dot{\bar{\phi}}}_{\text{source term}}, \quad \Phi_k : \text{curvature perturbations}$$

The EoM is unstable when the effective frequency

- becomes negative \Rightarrow tachyonic instability
- is oscillating \Rightarrow parametric resonance

Kofman et al. hep-ph/9704452; Felder, Kofman hep-ph/0606256

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Instability exists except for a free theory where $V''(\phi) = m^2$.

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The size of fluctuations is determined by the **density contrast**:

$$\delta_\rho(\vec{x}, t) \equiv \frac{\rho(\vec{x}, t) - \bar{\rho}(t)}{\bar{\rho}(t)}$$

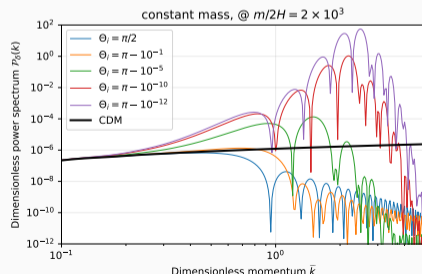
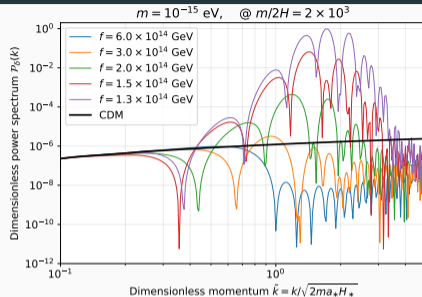
The **power spectrum (two-point function)** determines the distribution of structures today:

$$\mathcal{P}_\delta(k) = \frac{k^3}{2\pi^2} \left\langle \left| \tilde{\delta}_\rho(\vec{k}, t) \right|^2 \right\rangle$$

After the parametric resonance the power spectrum can reach to $\mathcal{O}(1)$ values:

Dense and compact ALP mini-clusters can also be formed in the pre-inflationary scenario!

Growth rate of the perturbations depend **exponentially** on $m_\phi/H|_{\text{osc}}$.



Breakdown of linearity and complete fragmentation

When the power spectrum becomes $\mathcal{O}(1)$, the linear perturbation theory **breaks** down, and the ALP field becomes completely **fragmented**. This regime can be studied by

- **Semi-analytically** via an energy conservation argument. Used for the Kinetic misalignment.

Fonseca et al. 1911.08472; CE, Servant, Sørensen, Sato 2206.14259

- **Fully numerically** using lattice simulations. Used for the non-periodic potentials.

Morgante et al. 2109.13823; Chatrchyan, CE, Koschnitzke, Servant 2305.03756

The non-linear effects **smoothens** out the power spectrum, so in the non-linear regime more efficient parametric resonance yields a power spectrum with smaller peaks.

For a given ALP mass m_ϕ and a production mechanism such as SMM, KMM, non-periodic etc..., there is a **critical** f_ϕ that yields the **most peaked** power spectrum, hence **most dense** structures.

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Fonseca et al. 1911.08472; CE, Servant, Sørensen, Sato 2206.14259

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Morgante et al. 2109.13823; Chatrchyan, CE, Koschnitzke, Servant 2305.03756

The non-linear effects **smoothens** out the power spectrum, so in the non-linear regime more efficient parametric resonance yields a power spectrum with smaller peaks.

For a given ALP mass m_ϕ and a production mechanism such as SMM, KMM, non-periodic etc..., there is a **critical** f_ϕ that yields the **most peaked** power spectrum, hence **most dense** structures.

Latetime evolution of the density contrast

For **sub-horizon** $k/a \gg H$ and **non-relativistic** $k/a \ll m$ modes, the density contrast evolution is

$$\ddot{\delta}_k + 2H\dot{\delta}_k + \left[\underbrace{\frac{c_{s,\text{eff}}^2(k/a)^2}{4} \frac{(k/a)^4}{m^2}}_{\text{"pressure" term}} - \underbrace{4\pi G\bar{\rho}}_{\text{gravitational instability}} \right] \delta_k = 0.$$

The scale at which the "pressure" term and gravitational instability becomes equal is called the **Axion Jeans scale**:

$$k_J(a) = (16\pi G a \bar{\rho})^{1/4} \sqrt{m} = 66.5 \times a^{1/4} \left(\frac{h^2 \Omega_\Theta}{h^2 \Omega_{\text{DM}}} \right) \sqrt{\frac{m}{10^{-22} \text{ eV}}} \text{ Mpc}^{-1}.$$

The behavior of the density contrast depends whether the mode is **above** or **below** the Jeans scale:

- **Modes above the Jeans scale** oscillate with a frequency given by the effective sound speed both in matter- and radiation-domination.
- **Modes below the Jeans scale** behaves like CDM. They grow logarithmically during the radiation era, and linearly during the matter era.

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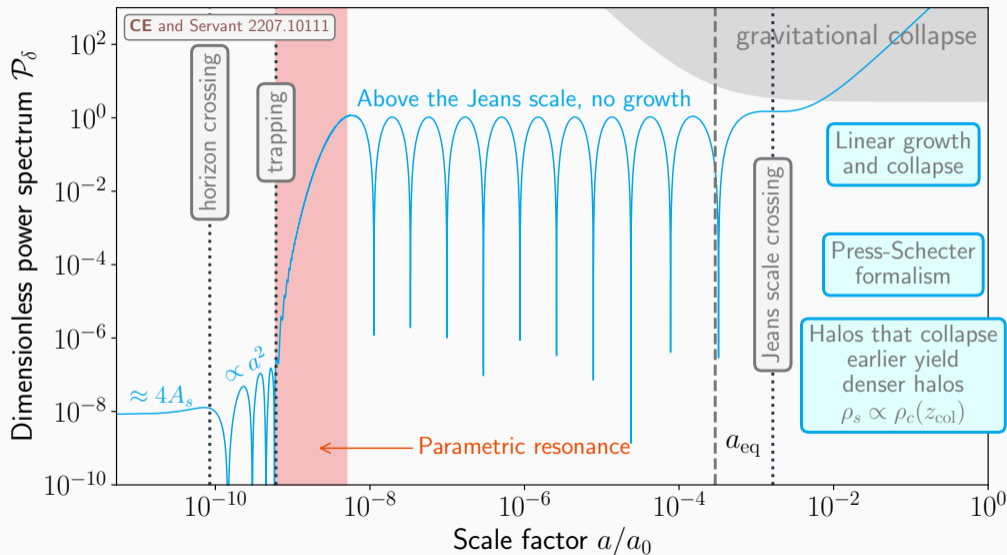
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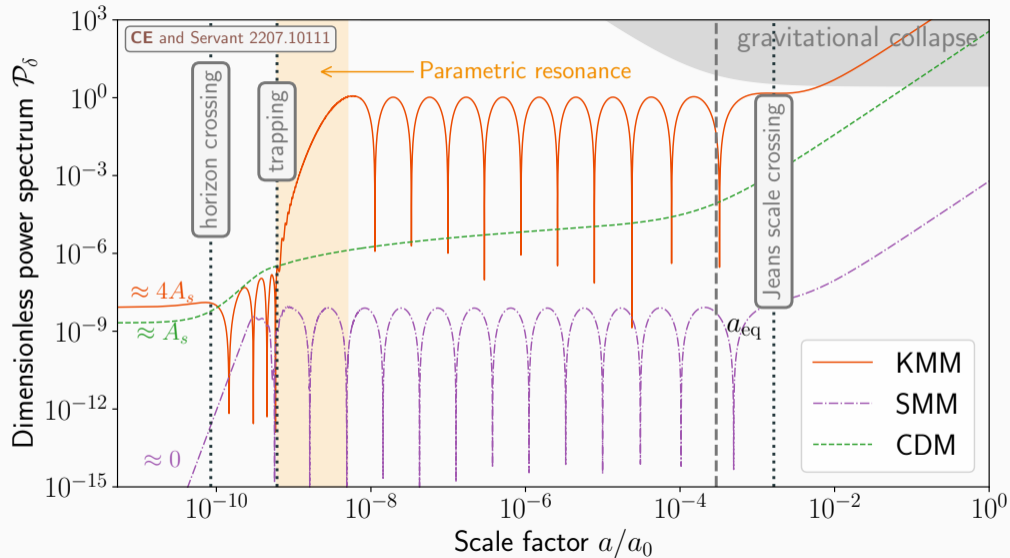
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Lifetime of a fluctuation mode



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Density profiles of dark matter halos

- Useful **parameters** to describe the dark matter halos:

$$\underbrace{\left. \frac{\partial \ln \rho(r)}{\partial \ln r} \right|_{r=r_s}}_{\text{scale radius}} = -2, \quad \underbrace{\rho_s = \rho(r = r_s)}_{\text{scale density}}, \quad \underbrace{M_s = \int_0^{r_s} d^3\vec{r} \rho(r)}_{\text{scale mass}} = 16\pi\rho_s r_s^3 \left(\ln 2 - \frac{1}{2} \right).$$

- In order to determine these parameters, we need to know the **density profile**.

CDM

On **all** scales, the profile is well-approximated by the Navarro-Frenk-White (NFW) profile

Navarro et al. astro-ph/9611107

$$\rho_{\text{NFW}}(r) = \frac{4\rho_s}{(r/r_s)(1+r/r_s)^2}.$$

ALP

The profile is **scale dependent**:

- Large scales:** NFW
- Small scales:** Soliton profile Schive et al. 1406.6586

$$\rho_{\text{sol}}(r) \approx \frac{2.9\rho_s}{\left(1 + \left(r/\sqrt{7}r_s\right)^2\right)^8} \Rightarrow \rho_s \propto m^6 M_s^4$$

- The scale density is closely related to the energy density at **collapse**:

$$\rho_s \propto \rho_c(z_{\text{col}}) \Rightarrow \text{Fluctuations that collapse } \mathbf{earlier} \text{ create } \mathbf{denser} \text{ halos.}$$

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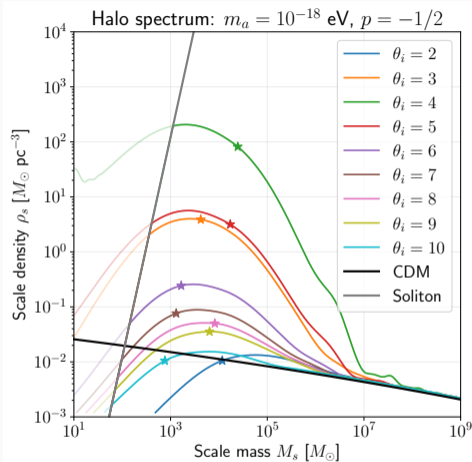
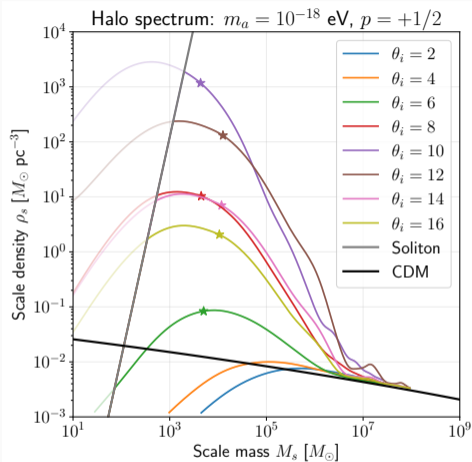
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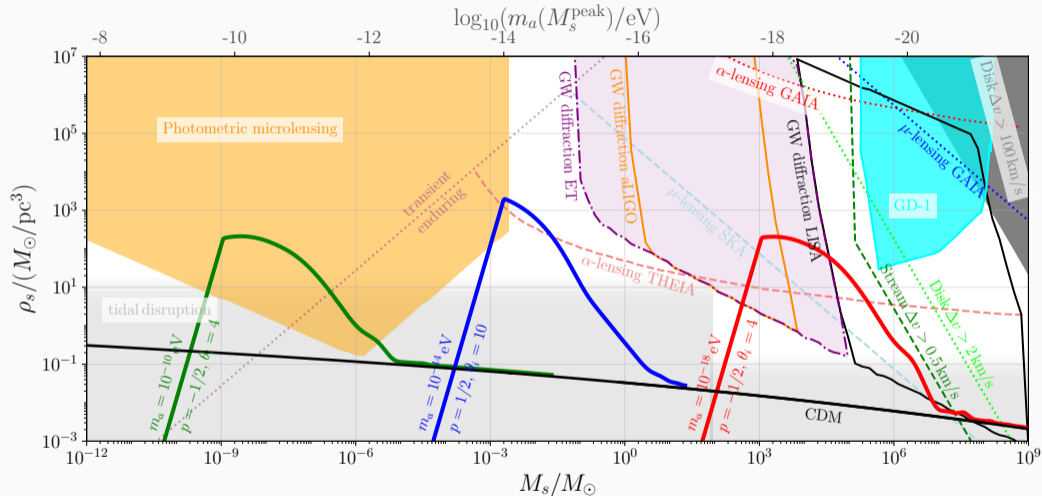
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Calculated semi-analytically using the **Excursion Set Formalism** assuming **NFW profile**, but setting the **soliton** line as a cutoff. Stars denote the local maxima of the **Halo mass function**.



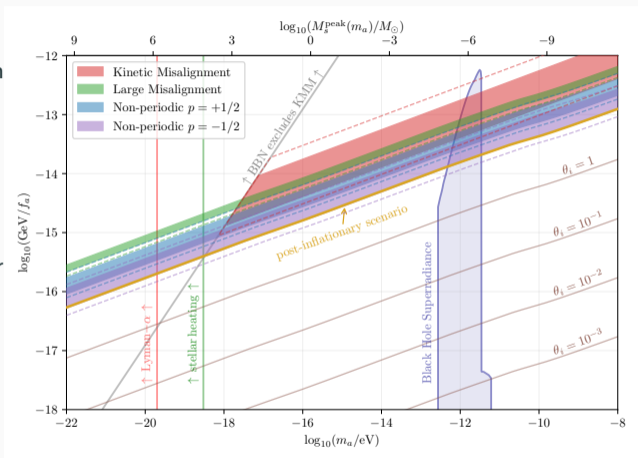
Experimental prospects from Tilburg et al. 1804.01991; Arvanitaki et al. 1909.11665; Ramani et al. 2005.03030

Shaded regions indicate the parameter space where parametric resonance **might** create halos with $\rho_s \gtrsim 10 M_\odot \text{pc}^{-3}$ which are more likely to survive **tidal stripping**

Arvanitaki et al. 1909.11665.

The “dense halo regions” in different production mechanisms mostly **overlap** with each other. So, it is **difficult** to infer the mechanism from observations.

However, observation of dense structures gives us information about the **decay constant** even when ALP does not couple to SM!



- The Standard Misalignment Mechanism is not **sufficient** to account for the correct dark matter abundance in the ALP parameter space where the experiments are most **sensitive**.
- This parameter space can be **opened** by considering models where the initial energy budget is **increased**, and the onset of oscillations is **delayed** from the conventional value $m_{\text{osc}}/H_{\text{osc}} \sim 3$.
- In these models which go **beyond** the standard paradigm, the fluctuations can grow **exponentially**, and **dense** ALP mini-clusters can be formed even in the pre-inflationary scenario.
- Our semi-analytical study predicts that there is a **band** on the (m_ϕ, f_ϕ) -plane where the dense structures can be formed, and the location of this band does **not depend** drastically on the production mechanism.
- The existence of this band allows us to **obtain** information about the **decay constant**, even if ALP does not couple to the Standard Model.

Thank you for listening!

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